Universality in the entropy change for the inverse magnetocaloric effect

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(Received 20 October 2012; published 22 April 2013)

A comprehensive study of the temperature (T) and magnetic field (H) dependence of magnetic entropy change (ΔSM) for different materials exhibiting inverse magnetocaloric effect (IMCE) is reported. We show that ΔSM follows a power-law dependence of H (ΔSM ∝ H^n; n is an exponent) for these compounds. In contrast to conventional magnetocaloric effect (CMCE), n is independent of H and T in the case of IMCE. As a result, a universal master curve can be constructed to describe ΔSM(T) of the IMCE systems for different H without rescaling the temperature axis. This is completely different from that reported for CMCE, where the rescaling of the temperature axis with the introduction of at least one reference temperature is needed for constructing a universal curve. The different universal behavior of IMCE is attributed to the constant value of n in any field and temperature, which is a generic feature of IMCE systems irrespective of their magnetic state and nature of phase transition. From the proposed phenomenological universal curve, one can extrapolate the magnetocaloric properties of IMCE systems in any temperature and magnetic field range, which would be helpful in designing controlled active magnetic refrigeration devices.

The study of the magnetocaloric properties of materials has been a subject of extensive research from both fundamental and application points of view.1–5 Magnetic refrigeration based on the magnetocaloric effect (MCE) is considered to be a viable alternative to conventional gas compression refrigeration technology.1 Furthermore by investigating magnetocaloric parameters of materials, one can acquire insightful understanding about complex magnetic phases present in the system, which may not be possible by just studying magnetization.6–9

Generally the application of a magnetic field causes the reduction in magnetic entropy of a refrigerant material and if the material is demagnetized adiabatically in subsequent steps, low temperature can be achieved. However, recent studies have revealed that an inverse effect can occur in some magnetic systems for which a magnetic field induced enhancement in magnetic configuration entropy is observed, and this is known as “inverse magnetocaloric effect” (IMCE).10–16 From a magnetic cooling perspective, it is worth mentioning that the adiabatic magnetization of materials exhibiting IMCE can generate cooling, and the efficiency of a refrigeration device can be improved by utilizing IMCE materials as “heat sinks” in composites with conventional magnetic refrigerants.10 Although IMCE is mostly observed in antiferromagnetic and ferrimagnetic materials, some ferromagnetic systems also show this effect due to martensitic transition.10,14,15

One of the important issues in studies related to magnetic refrigeration is to understand how the MCE of a material at different temperatures evolves with applied magnetic fields.1 For instance, a detailed analysis of the field dependence of MCE can provide useful information about the performance of a refrigerant for magnetic field ranges used in actual refrigeration cycles. Beside this, such a study can also be helpful to get deeper understanding of the nature of magnetic phase transitions and phase coexistence in the material.6–9 The magnetic field dependence of the magnetocaloric parameters has been shown to be associated with the intricate nature of magnetic phase transition and can be parametrized by critical exponents governing the transition.17–21 Recently, Franco et al. have introduced a method of using a “universal master curve” to describe the temperature dependence of magnetic entropy change [ΔSM(T)] in different applied magnetic fields for conventional magnetocaloric effect (CMCE).17,18 This method is valid when the magnetic transition in the material is of second-order type in nature. According to these studies, all ΔSM(T) curves near transition temperature (Tc) for different applied magnetic fields for a ferromagnetic (FM) system will collapse onto a universal master curve, when ΔSM(T) is normalized to its peak value and the temperature axis is rescaled as17

$$\theta = (T - T_c)/(T_r - T_c),$$

with T_r being a reference temperature corresponding to a certain fraction f that satisfies ΔSM(T_r)/ΔSM(T_c) = f.17,18 For systems with coexistence of more than one FM phase, two reference temperatures have to be used in the definition of θ to construct a universal curve.18 It is found that the construction of a universal curve using this method is not valid when CMCE arises due to the first-order phase transition.22 This idea of such universality has been extensively verified for different kinds of ferromagnetic systems showing CMCE as a result of the second-order transition and it has also been theoretically well grounded.17–22 However, little attention has been paid to systems exhibiting IMCE. As the IMCE materials are potentially important components in magnetic refrigeration, it is essential to gain a clear understanding of the temperature and field dependences of ΔSM in these systems. Most recently, our preliminary study has revealed that a universal behavior can exist in antiferromagnetic (AFM) systems showing IMCE.23 That research was limited to only one class of materials (manganites), and the analysis of the IMCE behavior was confined up to a 3-T magnetic field, below the critical field (3.5 T) at which the first-order-like transition occurred for those particular systems.23 This leads to the emergence of
the following important questions that need to be addressed in order to get comprehensive understanding of the universal behavior of IMCE:

(i) Is a universal behavior attributed to the antiferromagnetic transition of an IMCE system?

(ii) Can a universal curve be constructed for materials undergoing a first-order structural or magnetic field induced transition?

(iii) Can a similar universal behavior exist in CMCE systems with antiferromagnetic correlation?

(iv) Does a universal curve exist for ferromagnetic materials exhibiting IMCE?

The overall aim of this paper is to address these outstanding questions through a systematic study of the magnetocaloric effect and universal behavior in three kinds of magnetic systems: (a) antiferromagnetic materials showing IMCE (antiferromagnetic manganites: La$_{0.17}$Ca$_{0.83}$MnO$_3$ and La$_{0.125}$Ca$_{0.875}$MnO$_3$); (b) materials showing an anti-ferromagnetic and ferromagnetic coexistence and CMCE (a self-doped manganite: LaMnO$_3$); and (c) ferromagnetic materials showing IMCE (a representative Heusler alloy: Ni$_{50}$Mn$_{36}$Sn$_{14}$).

Polycrystalline samples of La$_{0.17}$Ca$_{0.83}$MnO$_3$ (LCMO-1) and La$_{0.125}$Ca$_{0.875}$MnO$_3$ (LCMO-2) were prepared by using a sol-gel technique followed by annealing at 1400 °C for 36 h. For comparison, we have also extended our study to self-doped La$_{0.04}$ (LMO), which was prepared by a standard solid-state reaction method. The powder x-ray diffraction (XRD) study confirmed the successful preparation of samples. All three samples are of orthorhombic structure. The XRD patterns of the samples have been shown in Fig. 1. The Ni$_{50}$Mn$_{36}$Sn$_{14}$ sample was prepared by the melt-spinning method. The details of the preparation and characterization of this sample have been reported elsewhere. A physical property measurement system (PPMS) equipped with vibrating sample magnetometer (VSM) was used for the magnetization study.

We investigated the temperature dependence of magnetization [$M(T)$] to probe the magnetic transitions in the samples. From $M(T)$ curves (measured in the presence of 0.02 T magnetic field) for both LCMO-1 and LCMO-2 [inset, Fig. 2(a)], it is clear that the samples undergo an antiferromagnetic transition at $T_N \sim 170$ and $125$ K, respectively. There is negligible irreversibility between $M(T)$ curves recorded in the zero field cooled and field cooled protocols. The reversibility of $M(T)$ curves can be an indication of the second-order nature of phase transition. We have also studied the isothermal magnetic field dependence of magnetization [$M(H)$] and checked $H/M$ versus $M^2$ (Arrott plots) obtained from $M(H)$ curves to get an idea about the nature of magnetic phase transitions in the samples. The representative $M(H)$ curves at some selected temperatures for LCMO-1 and LCMO-2 are shown in Figs. 2(a) and 2(b), respectively. As an example, the Arrott plots for LCMO-2 are given in the inset of Fig. 2(b). It appears that the Arrott plots have positive slopes up to magnetic fields of $H_{cric} \sim 3.5$ T (critical field) and then the slope gradually becomes negative. Thus according to Banerjee’s criteria the transition in the case of La$_{1-x}$Ca$_x$MnO$_3$ ($x \sim 0.83, 0.875$) may be considered as second order when the applied magnetic field is below $3.5$ T.$^{23,25}$ The observed second-order nature of the transition can be an intrinsic property of the material. However, the presence of quenched disorder can render a first-order transition to a continuous second-order-like transition in the case of doped manganite systems.$^{26}$ Under such a situation the observed second-order nature of the transition can arise due to extrinsic factors, not related to the intrinsic property of the system. This possibility cannot be ruled out for our present samples. Beyond the $3.5$-T field, the gradual slope change of Arrott plots towards negative value can be attributed to the tendency of a magnetic field induced first-order transition and we denote this field as $H_{cric}$ hereafter. Negligible field hysteresis is observed in $M(H)$ curves especially below $H_{cric}$.

The magnetic entropy change ($\Delta S_M$) was calculated from the isothermal $M(H)$ curves using the following Maxwell’s equation:

$$\left[ \frac{\partial S(T,H)}{\partial H} \right]_T = \left[ \frac{\partial M(T,H)}{\partial T} \right]_H. \quad (2)$$

The $-\Delta S_M(T)$ curves for LCMO-1 and LCMO-2 at different magnetic fields (0.1–5 T) are shown in Fig. 3(a) and its inset. The positive value of $\Delta S_M$ below $T_N$ is signature of IMCE due to antiferromagnetic transition.$^{24}$ The value of maximum entropy change increases with applied magnetic fields.

In general, the magnetic field dependence of $\Delta S_M$ for a magnetic material can be expressed as

$$\Delta S_M \sim H^n, \quad (3)$$

where $n$ is called a local exponent.

For LCMO-1 and LCMO-2, $\ln |\Delta S_M|$ versus $\ln H$ curves are linear [Figs. 3(b) and 3(c)] indicating $\Delta S_M$ follows a power-law dependence of $H$ according to Eq. (3). Interestingly, the value of $n$ is $\sim 2$ for the entire temperature and magnetic field range ($n$ is calculated from the slope of linear $\ln |\Delta S_M|$ versus $\ln H$ plots for different temperatures). In the case of FM systems showing CMCE, the value of $n$ is strongly temperature dependent.$^{21}$ It is $\sim \frac{1}{2}$ near the transition temperature ($T_C$) and $\sim 1$ well below $T_C$ for a ferromagnetic system. This value reaches 2 at temperatures well above $T_C$ in the paramagnetic (PM) regime. In addition, $n$ changes with magnetic field for those materials.$^{17-21}$ Thus the magnetic field

![Fig. 1. (Color online) X-ray diffraction pattern of La$_{0.17}$Ca$_{0.83}$MnO$_3$ (LCMO-1) and La$_{0.125}$Ca$_{0.875}$MnO$_3$ (LCMO-2). Inset: x-ray diffraction pattern of LaMnO$_3$.](134420-2)
dependence of $\Delta S_M$ is entirely different in the case of an IMCE material in comparison with systems exhibiting CMCE. To better illustrate the magnetic field and temperature dependences of $n$, we have determined $n(H,T)$ using the formula

$$n = \frac{d \ln |\Delta S_M|}{d \ln H}. \quad (4)$$

It is found that $n$ is $\approx 2 \pm 0.02$ regardless of the measurement temperature and magnetic field for both the samples, when the applied field is below $H_{\text{cric}}$, as for example, $n(H)$ for LCMO-1 has been shown in Fig. 3(d). However, the value of $n$ becomes $\approx 2 \pm 0.1$ (fluctuation slightly increases) at applied fields higher than $H_{\text{cric}}$ [Fig. 3(d)]. This can be associated with the onset of a magnetic field induced first-order transition. As $n$ is constant in the entire temperature range for magnetic fields, with a very small fluctuation especially below $H_{\text{cric}}$, the normalized $\Delta S_M$ (normalized to the value obtained for maximum magnetic field) versus $H$ plots obtained for different temperatures collapse onto the single curve [Figs. 3(e) and 3(f)]. The collapse of linear $\ln \frac{\Delta S_M}{\Delta S_{\text{Max}}}$ versus $H$ curves onto a single curve is shown in the insets of Figs. 3(e) and 3(f). Consequently $\Delta S_M(T)$ (normalized to maximum value, i.e., $\Delta S_M$ at antiferromagnetic transition temperature, $\Delta S_{\text{Max}}$) for different magnetic fields below $H_{\text{cric}}$ can also be collapsed onto a universal curve contrary to the situation in CMCE materials, for which one needs to rescale the temperature axis and define the reference temperature to construct a universal curve. Figures 3(g) and 3(h) show a universal $\Delta S_M(T)$ curve for LCMO-1 and LCMO-2, respectively, where the $y$ axis represents $\Delta S_M/\Delta S_{\text{Max}}$ and the $x$ axis is $T/T_N$. In this case, we restrict our analysis to the magnetic field range 0.1–5 T, which is below the $H_{\text{cric}}$.

To quantify the uncertainty associated with the collapsing of $\Delta S_M(T)$ curves, we have defined a dispersion $d$ corresponding to each point in the universal curve as

$$d = 100 \times \frac{W}{(\Delta S_M/\Delta S_{\text{Max}})}, \quad (5)$$

where $W$ is the vertical deviation of each entropy curve with respect to its mean value. For both systems, $d$ is found to be less than 6% for most of the points. It has been emphasized in different studies that the measurement uncertainty is always present in indirect measurement of magnetocaloric parameters. Pecharsky et al. have quantified measurement uncertainty associated with the calculation of $\Delta S_M$ using Maxwell’s equation [Eq. (3)] as $\sim 20\%$ near transition and it is even higher below a transition temperature. This kind of measurement uncertainty can give rise to a finite value of $d$ for constructing a universal curve. Generally, for the systems showing CMCE, $d$ corresponding to a universal curve is found to be always less than 30%. In our case, $d$ ($<6\%$) is within the reported value obtained for different magnetic materials. It is even better than the calculated $d$ ($\sim 9\%$) for other ferromagnetic manganese published in an earlier work. It should be mentioned that we have also constructed a universal curve including $\Delta S_M(T)$ obtained for magnetic fields beyond $H_{\text{cric}}$ (the field range of 0.1–5 T). In that case, the obtained maximum $d$ is $\sim 15\%$, which is well below the typical $d$ associated with universal curves for different materials. Thus the construction of universal curve can be possible for these systems even beyond $H_{\text{cric}}$. As an example, the collapse of $\Delta S_M/\Delta S_{\text{Max}}$ versus $T/T_N$ curves for 0.1–5 T in the case of LCMO-1 is shown in Fig. 4(a).

Recently, the large IMCE has been reported in MnNiGe$_{0.915}$Al$_{0.085}$, which is attributed to a phase transition from hexagonal FM to orthorhombic AFM state. We have checked that a universal curve can also be constructed without rescaling the temperature axis to describe its $\Delta S_M(T)$ (Ref. 16) similar to LCMO-1 and LCMO-2.

From the temperature and magnetic field dependences of these IMCE materials, it can be concluded that IMCE in these antiferromagnetic systems has a unique universal behavior. Unlike the cases of FM systems showing CMCE, the local exponent, $n$, is independent of temperature and magnetic field for AFM materials, which allows one to construct a universal master curve without rescaling the temperature axis as indicated in an earlier study. Interestingly, the universal behavior for these systems is valid even for the magnetic field induced first-order transition.

Now let us discuss the origin of such a different universal behavior of magnetic entropy change for these AFM materials. Since $\Delta S_M$ is calculated from the magnetic field dependence...
of magnetization, we have analyzed the \( M(H) \) curves (below \( H_{\text{cric}} \)) for the present \( \text{La}_{1-x}\text{Ca}_x\text{MnO}_3 \) samples in the temperature range relevant to IMCE. A parameter \( \omega \) is defined as \( \omega = M/T \). It has been observed that all \( \omega \) (normalized to its maximum value) versus \( H \) curves for a given material can be collapsed onto a single curve as the magnetic field dependence of \( \omega \) follows a scaling relation: \( \omega \sim H^\xi \), where \( \xi \) is a system-dependent constant. We have evaluated the value of \( \xi(H,T) \) by using the following equation:

\[
\xi = \frac{d \ln |\omega|}{d \ln H}.
\]

For LCMO-1 and LCMO-2, \( \xi \) is found to be \( \sim 1 \pm 0.02 \) when the field is below \( H_{\text{cric}} \) and it becomes \( \sim 1 \pm 0.1 \) at the magnetic field higher than \( H_{\text{cric}} \). For example, calculated \( \xi(H,T) \) for LCMO-1 has been shown in the top inset of Fig. 4(b). The collapsing of the normalized \( \omega \) versus \( H \) curves in the magnetic field range below \( H_{\text{cric}} \) and in the entire magnetic field range (0–5 T) for that sample has been given in Fig. 4(b) and its bottom inset, respectively. As \( \Delta S_M \) is related to \( M \) and \( H \) via Eq. (2), the power-law dependence of \( \Delta S_M \) with magnetic field \( (\Delta S_M \sim H^n \text{ with } n \approx \xi + 1) \) is easily understood. For these two samples the scaling behavior of \( \omega \) with \( H^\xi \) results in their temperature and magnetic field independence of \( n \) (\( \approx \xi + 1 \)) and hence the collapsing of \( \Delta S_M/\Delta S_{\text{Max}} \) versus \( T/T_N \) for all different magnetic fields is observed. The estimated value of \( \xi \) is almost the same for both LCMO-1 and LCMO-2. Therefore these two samples have nearly the same value of \( n \) and their temperature dependences of \( \Delta S_M \) obtained for different applied fields fall onto the
In this regard, we have investigated universal behavior of MCE in the case of self-doped LaMnO$_3$$_{0.4}$ (LMO). This system shows CMCE with an appreciably large $\Delta S_M$ arising due to a magnetic transition from PM to a magnetic state where AFM develops along with FM.$^9$ Our recent neutron diffraction study confirms the presence of AFM correlations in this material below transition temperature ($T_p$), which greatly influences its magnetocaloric property.$^9$ The details of magnetocaloric and magnetic properties of this sample are published elsewhere.$^9$ In contrary to LCMO-1 and LCMO-2, it appears that the normalized $\Delta S_M(T)/\Delta S_{M_{\text{Max}}}$ and $T/T_p$ (where $T_p$ being temperature corresponding to $\Delta S_{M_{\text{Max}}}$) plots for different magnetic fields cannot be collapsed onto a universal curve [Fig. 5(a)] for this compound. The universal curve can be obtained for LMO only when the temperature axis is rescaled, similar to the case of ferromagnetic CMCE systems as proposed by Franco et al.$^{17}$ [Fig. 5(b)]. From this study, it can be inferred that the construction of a universal curve without rescaling the temperature axis can be possible for IMCE materials only. Even for the compounds with AFM correlation showing CMCE, the temperature axis has to be rescaled to construct a universal $\Delta S_M(T)$ curve.

Finally, we have analyzed the magnetocaloric data of Ni$_{50}$Mn$_{36}$Sn$_{14}$. $^{14}$ It is well established that Ni-Mn-Sn is a...

![Figure 4](image_url)

FIG. 4. (Color online) (a) $\Delta S_M(T)/\Delta S_{M_{\text{Max}}}$ versus $T/T_N$ obtained for entire temperature range (0.1–5 T) in the case of LCMO-1. (b) $\omega/\omega_{\text{max}}$ versus $H$ for different temperatures (70–250 K) fall into a single curve for LCMO-1 when magnetic field is below $H_{\text{cric}}$ (0–3 T). Here $\omega_{\text{max}}$ is the value of $\omega$ at 3-T magnetic field. Top inset: magnetic field dependence of $\xi$ [calculated using Eq. (6)] at different temperatures. Bottom inset: $\omega/\omega_{\text{max}}$ versus $H$ in entire temperature range. The value of $\omega$ at 5-T magnetic field is taken as $\omega_{\text{max}}$. (c) $\Delta S_M(T)/\Delta S_{M_{\text{Max}}}$ versus $T/T_N$ curves for all different magnetic fields collapse onto the same universal master curve in the cases of both LCMO-1 and LCMO-2.

![Figure 5](image_url)

FIG. 5. (Color online) (a) $\Delta S_M(T)$ curves obtained at different magnetic fields for LaMnO$_3$$_{0.4}$ (LMO). (b) $\Delta S_M(T)/\Delta S_{M_{\text{Max}}}$ versus $T/T_p$ [$T_p$ being temperature corresponding to the peak of $\Delta S_M(T)$] curves measured for different magnetic fields do not fall onto the same curve in the case of LaMnO$_3$$_{0.4}$ (LMO). (c) $\Delta S_M(T)/\Delta S_{M_{\text{Max}}}$ curves collapse onto universal curve for LMO when temperature axis is rescaled according to Eq. (1).
ferromagnetic system exhibiting a giant IMCE, due to a first-order phase transition from the austenite to martensite state. In particular, Ni$_{50}$Mn$_{37}$Sn$_{13}$ undergoes an austenite-martensite transition at $\sim 165$ K, which is associated with a large IMCE ($\Delta S_{\text{M}} \sim 20/\text{kg K}$ for 5-T magnetic field). The magnetic and magnetocaloric properties of this system have been discussed in detail in an earlier study. The temperature dependences of its $\sim \Delta S_M$ for different magnetic fields are shown in Fig. 6(a), which clearly indicates the occurrence of IMCE in the temperature range 150–175 K. We have found that the $\Delta S_{\text{M}}$ follows the power-law dependence of $H$ ($\Delta S_M \sim H^n$) in the temperature regime associated with IMCE, with a constant exponent $n \approx 1.1 \pm 0.12$. This is reflected in the collapse of all linear $\ln(\Delta S_M/\Delta S_{\text{ST}})$ versus $\ln H$ curves onto a single linear curve [inset, Fig. 6(b)]. As a result, all $\Delta S_M(H)$ curves (normalized to the value at the highest magnetic field, 5 T) can be collapsed onto a single curve [Fig. 6(b)] in the temperature range 150–175 K. In addition to this, all of its $\Delta S_M/\Delta S_{\text{max}}$ curves also fall on a universal curve in that temperature range without rescaling the temperature axis [Fig. 6(c)]. The calculated value of maximum $d$ is $\sim 15\%$ in this case. We have also examined the validity of the proposed universal curve for the magnetocaloric data of several other IMCE materials, including Ni$_{50}$Mn$_{37}$Sn$_{13}$ [Ref. 14], Ni$_{50}$Pt$_{17}$Mn$_{17}$Sn$_{13}$ and Ni$_{50}$Pt$_{17}$Mn$_{17}$Sn$_{13}$ [Ref. 31], Ni$_{50}$Mn$_{37}$Sn$_{13}$ [Ref. 10], (Ni,Co)$_{50}$Mn$_{37}$Sn$_{13}$ (Co $\sim 1\%$) and (Ni,Fe)$_{50}$Mn$_{37}$Sn$_{13}$ (Fe $\sim 1\%, 3\%$) [Ref. 32]. These results clearly point out that the construction of a universal curve to describe $\Delta S_M(T)$ without rescaling the temperature axis would be a common feature for IMCE materials irrespective of their magnetic states and nature of phase transition. Nevertheless, we note that the validity of the proposed universal behavior may not hold for systems showing a considerable shift in the IMCE peak with magnetic field, such as FeRh.

To summarize, we have systematically investigated the temperature and magnetic field dependences of IMCE in different antiferromagnetic and ferromagnetic materials. We find that in contrast to the materials showing CMCE, it is possible to construct a universal master curve to describe $\Delta S_M(T)$ of IMCE systems for different $H$ without rescaling the temperature axis. Unlike the case of CMCE, the proposed universal behavior is found to be valid even when IMCE is associated with the first-order phase transition. For such IMCE compounds, $\Delta S_M$ follows a power-law dependence of magnetic field: $\Delta S_M \sim H^n$, where $n$ is independent of $H$ and $T$. The construction of a universal curve will be helpful to understand the magnetocaloric response of IMCE materials in any temperature and magnetic field ranges, which would be imperative to judge their prospects in actual magnetic refrigeration devices.

We acknowledge Professor V. Franco of Sevilla University for his useful comments. We would like to thank Dr. T. L. Phan and Professor S. C. Yu of Chugung Buk National University for providing the magnetocaloric data of Heusler alloys for verifying our proposed universal behavior. Research at USF was supported by DOE BES Physical Behavior of Materials Program through Grant No. DE-FG02-07ER46438. Research at SNBNCBS was supported by DST, Govt. of India sponsored unit for Nanoscience under UNANST-II. M.H.P. acknowledges the support from the Florida Cluster for Advanced Smart Sensor Technologies (FCASST).

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31 S. C. Yu and T. L. Phan (private communication).